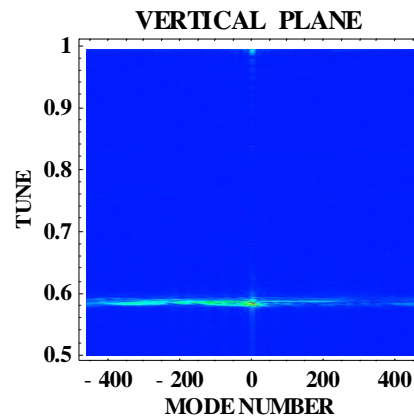
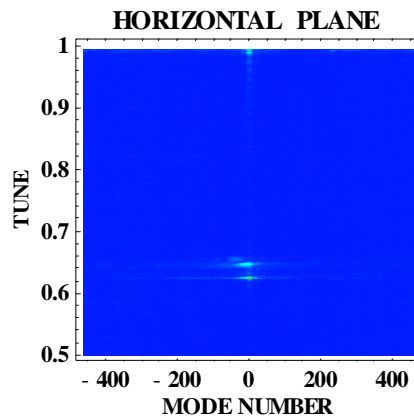
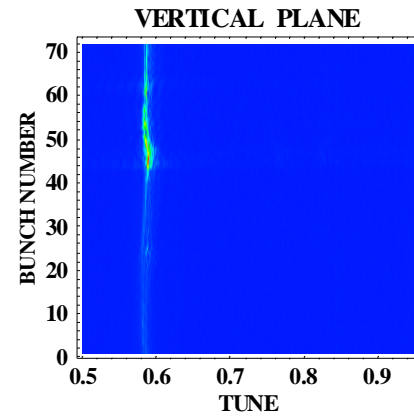
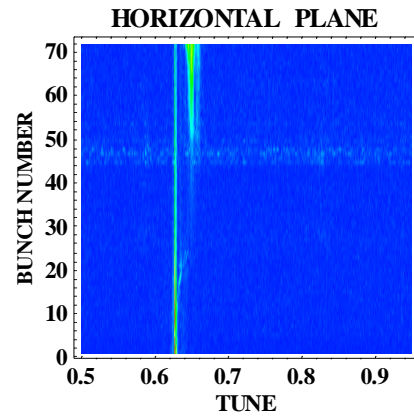
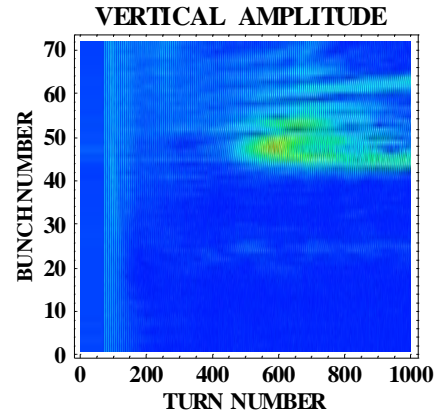
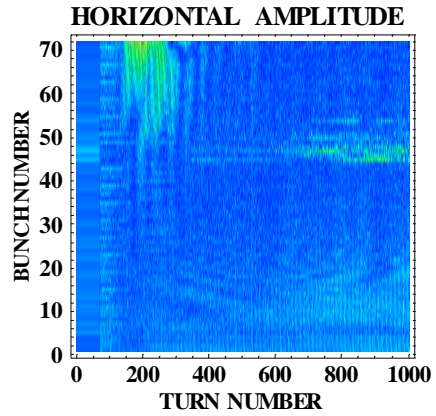


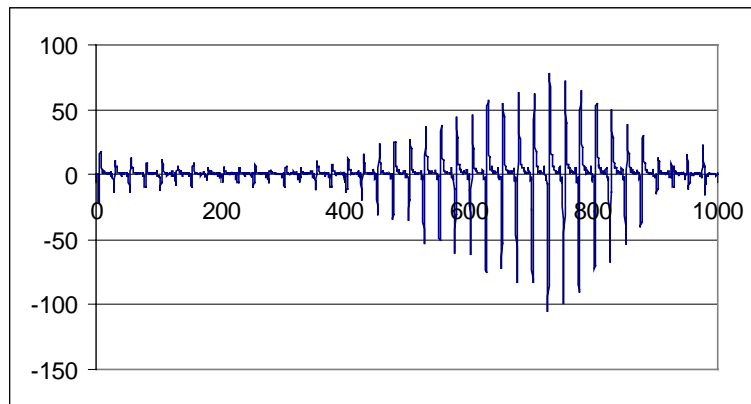
The Electron-Cloud Instability in the SPS

K. Cornelis

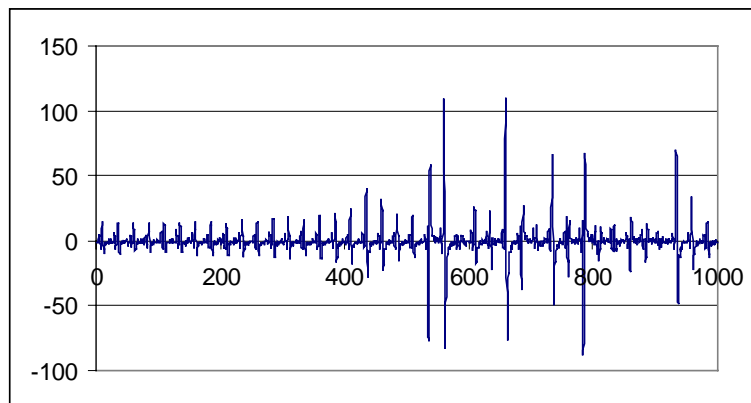
G. Arduini, F. Zimmermann, G.
Rumolo, R. Jones, L. Jensen.



The instability



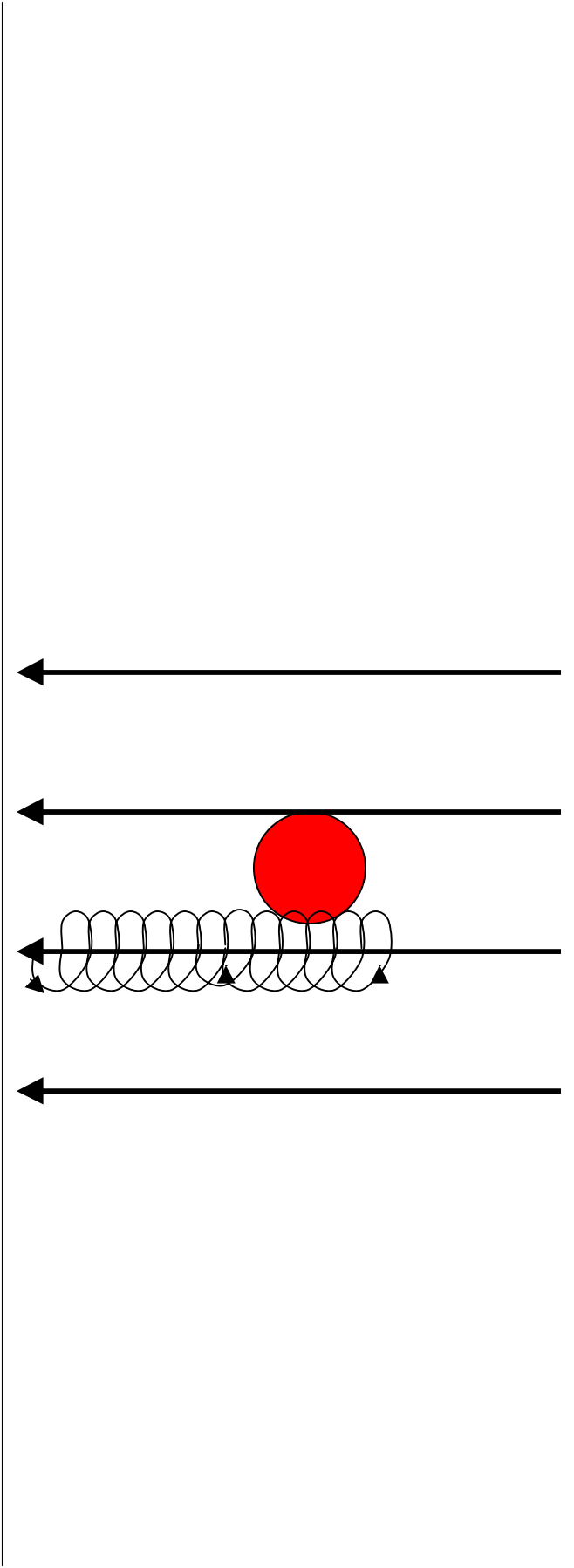
Snapshot of the horizontal
instability



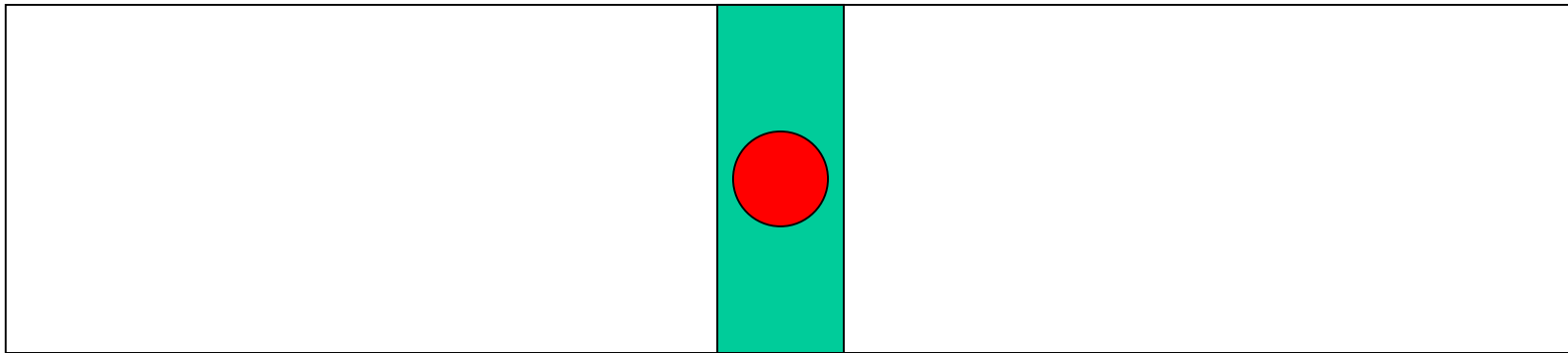
Snapshot of the vertical
instability

Sumarising

- In the Horizontal plane the e-cloud provokes a fast growing coupled bunch instability of low order. Growth rate is ~ 50 turn. Does not change much with intensity.
- In the vertical plane the instability looks like single bunch instability. Growth rate : ~ 500 turns just above threshold going to ~ 100 turns at two times the threshold.



How to understand this ?



In the SPS the electron cloud is created in the dipoles. It has the shape of a vertical ribbon. The horizontal density distribution depends on the bunch intensity, the bunch size and the magnetic field

A simple description of coupled Bunch motion

$$\frac{d^2}{dt^2} X_1 + \omega^2 \cdot X_1 := 0$$

.....

$$\frac{d^2}{dt^2} X_n + \omega^2 \cdot X_n := 0$$

$$\frac{d^2}{dt^2} X_{n+1} + \omega^2 \cdot X_{n+1} := k \cdot (X_{n+1} - X_n)$$

....

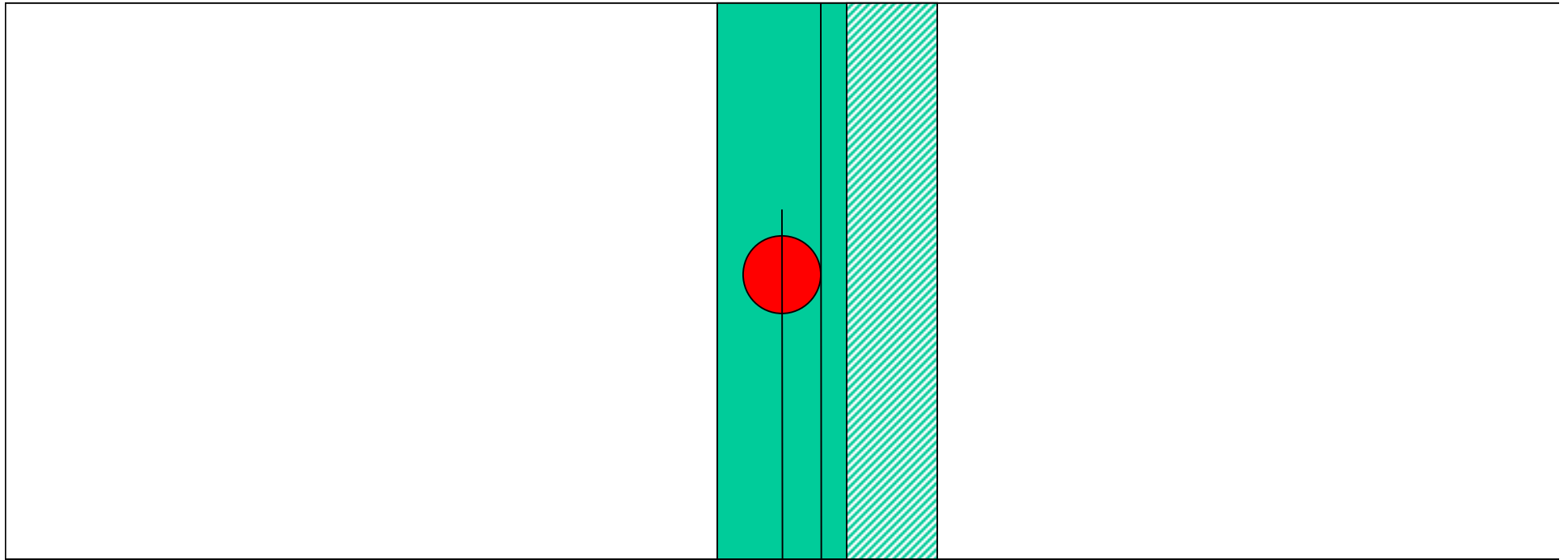
$$\frac{d^2}{dt^2} X_{72} + \omega^2 \cdot X_{72} := k \cdot (X_{72} - X_{71})$$

TWO Eigen
frequencies :

$$0 := (\omega^2 - k - \Omega^2)^{72-n} \cdot (\omega^2 - \Omega^2)^{72-n}$$

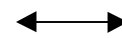
$$\Omega^2 := \omega^2$$

$$\Omega^2 := \omega^2 - k$$



$$F = \frac{2\rho e}{2\epsilon_0}$$

x



2x

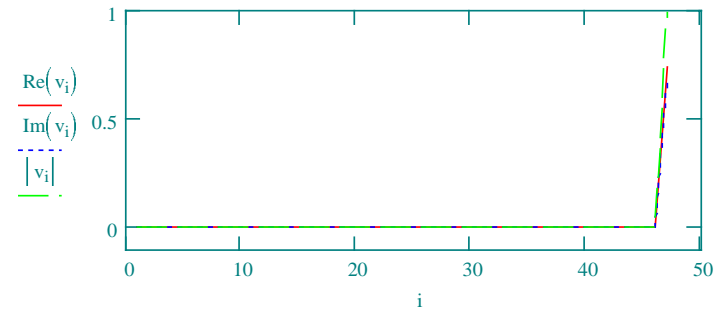
$$\frac{d^2 P^\perp}{dx ds} = \frac{\rho e}{\epsilon_0 c P}$$

$$dQ = \frac{\rho \langle \beta \rangle L}{\epsilon_0 26.10^9}$$

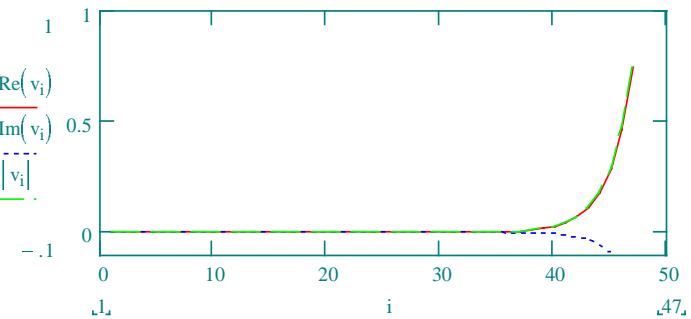
eigenvectors

p = 46

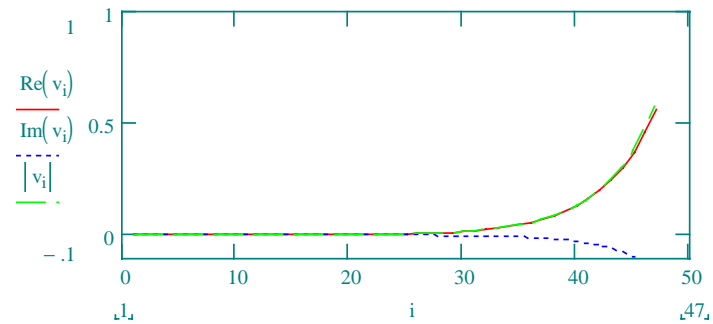
N=1



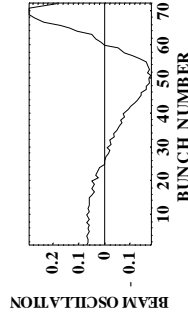
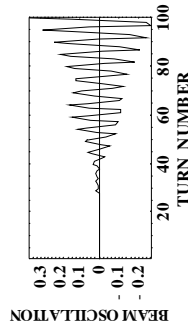
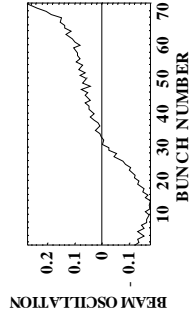
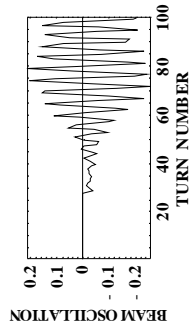
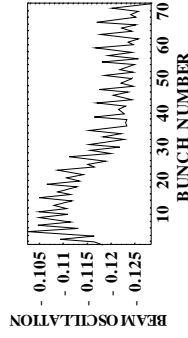
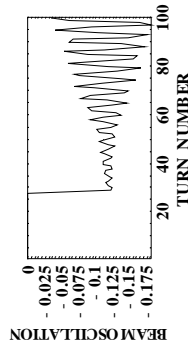
N=2



N=3



HORIZONTAL PLANE



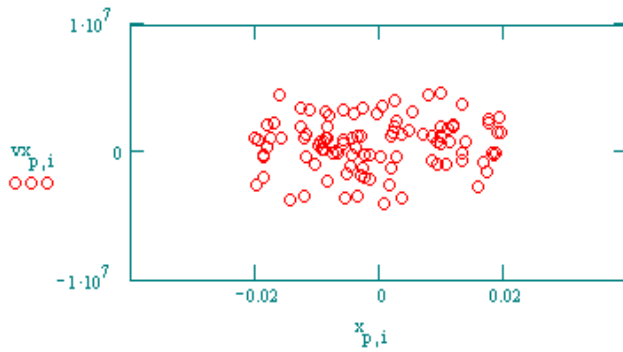
Electron phase space during bunch passage

p := FRAME

$N = 5 \cdot 10^{10}$

H

B = 0.1

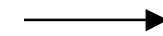
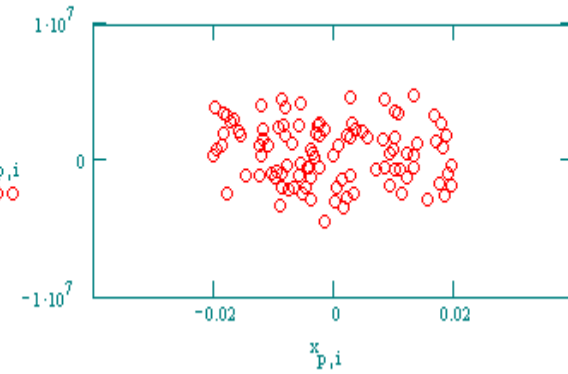


p := FRAME

$N = 5 \cdot 10^{10}$

H

B = 0.1

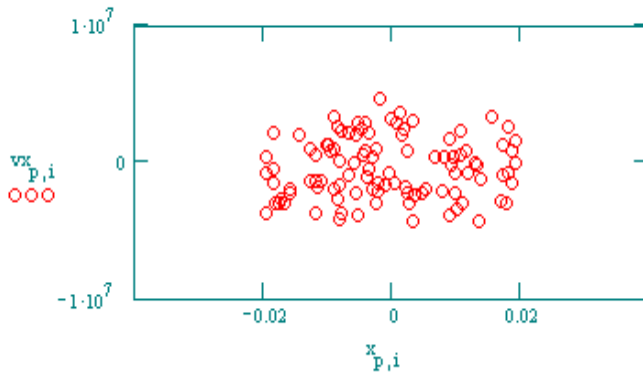


p := FRAME

$N = 5 \cdot 10^{10}$

H

B = 0.1

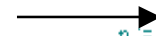
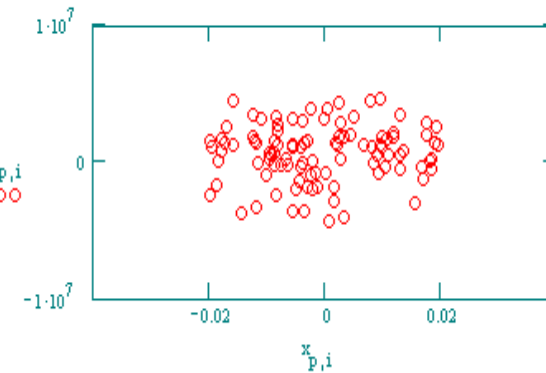


p := FRAME

$N = 5 \cdot 10^{10}$

H

B = 0.1



HORIZONTAL PLANE

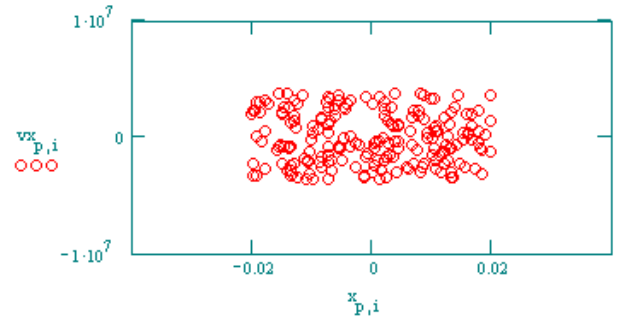
Electron phase space during bunch passage

p :=FRAME

$N = 8 \cdot 10^{10}$

H

B = 0

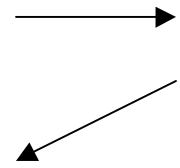
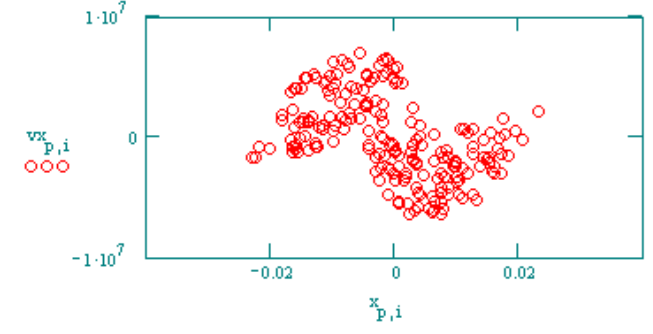


p :=FRAME

$N = 8 \cdot 10^{10}$

H

B = 0

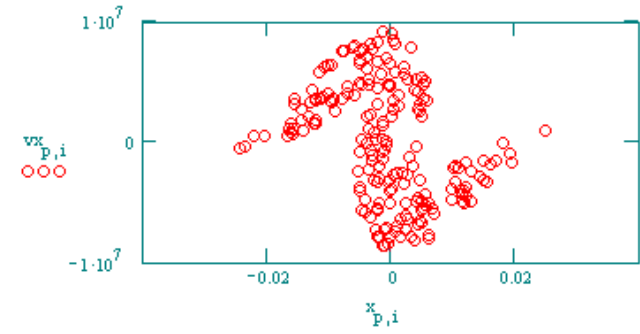


p :=FRAME

$N = 8 \cdot 10^{10}$

H

B = 0

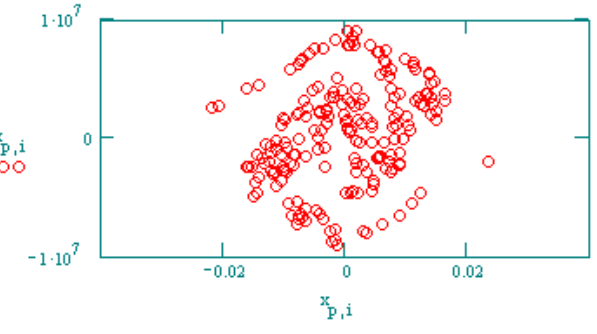


p :=FRAME

$N = 8 \cdot 10^{10}$

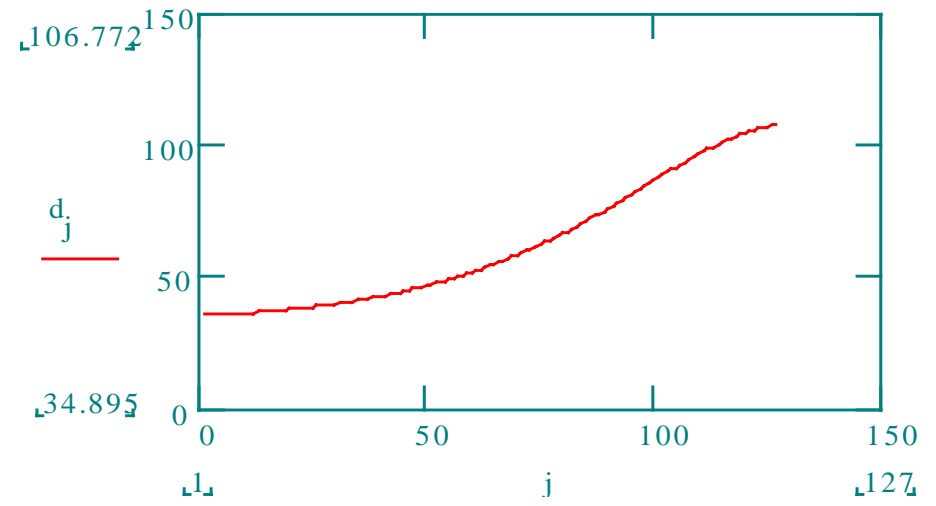
H

B = 0

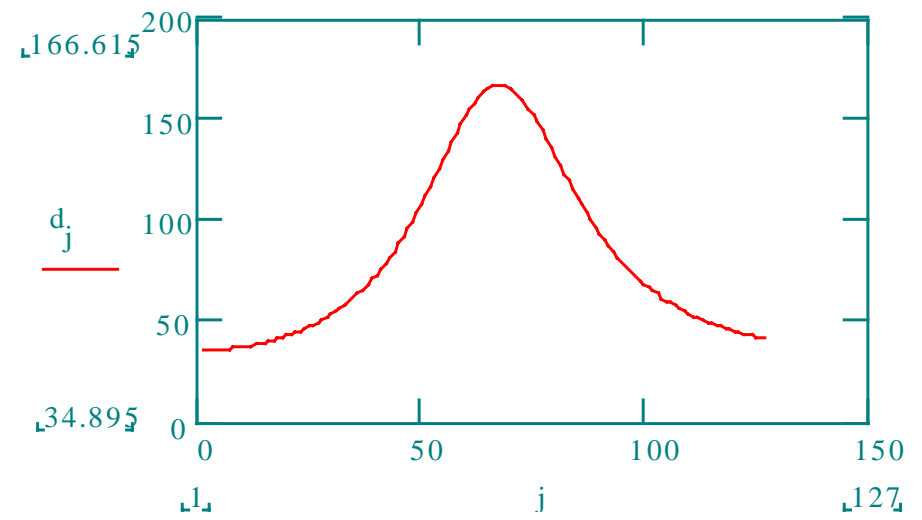


VERTICAL PLANE

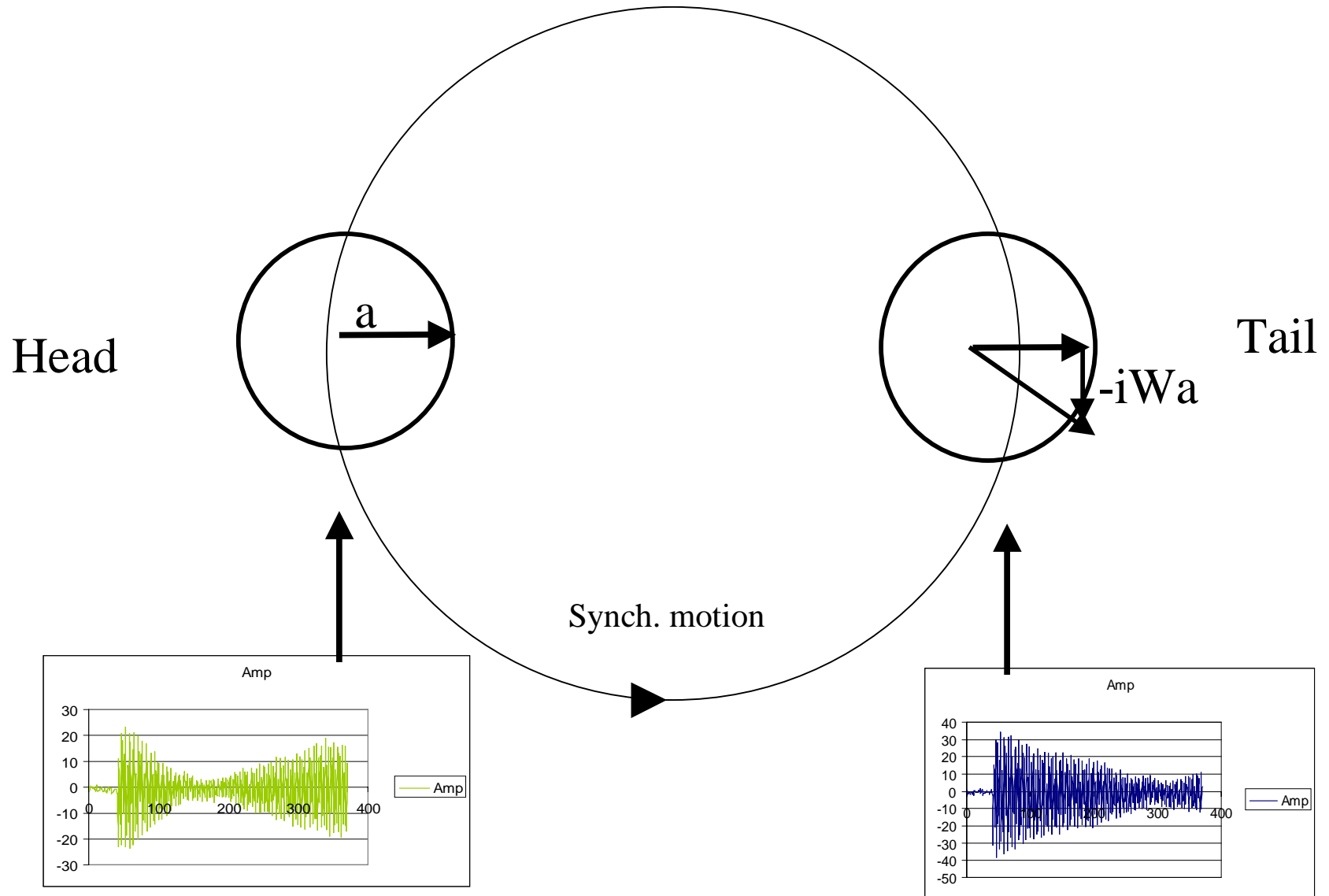
$2.5 \cdot 10^{10}$



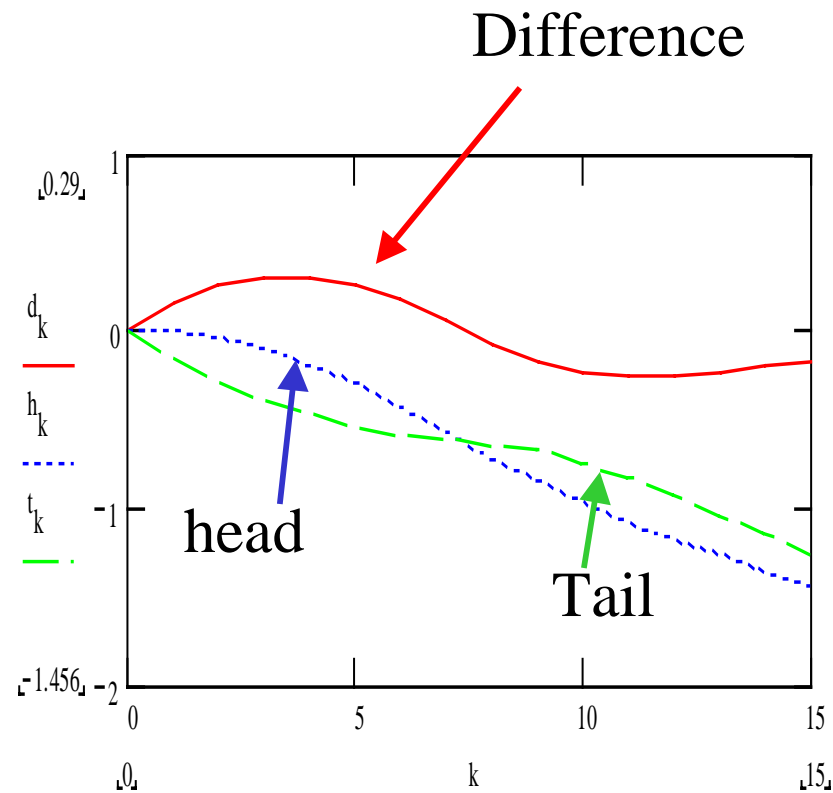
$8 \cdot 10^{10}$



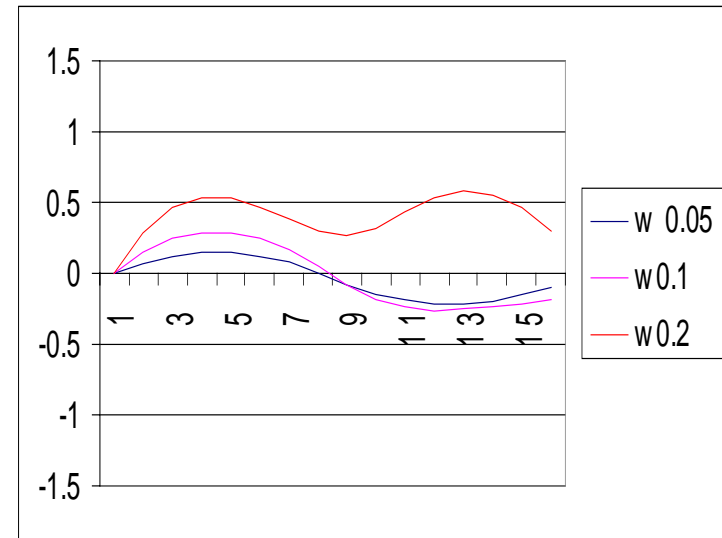
Phase difference due to impedance



Phase advance and Impedance



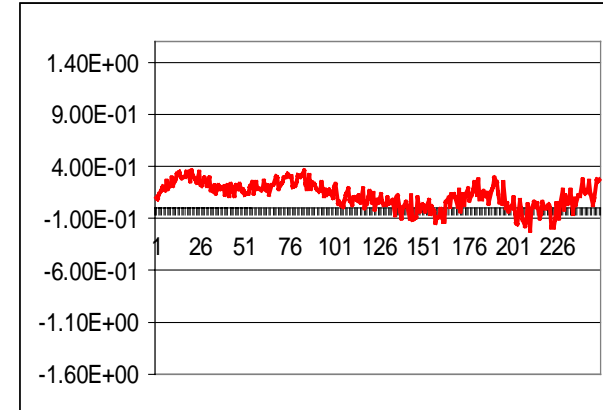
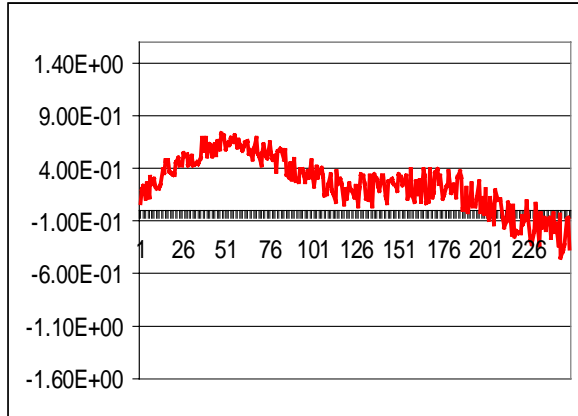
Phase advance of head and tail after kick over 1 synchrotron period



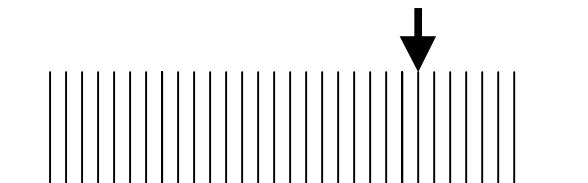
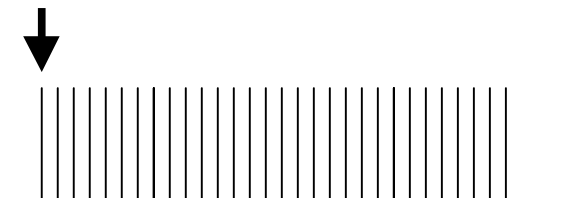
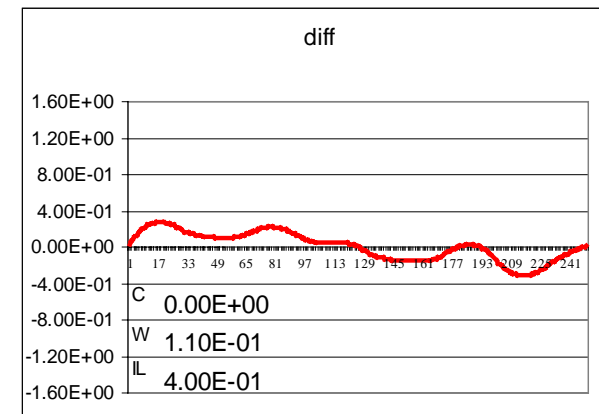
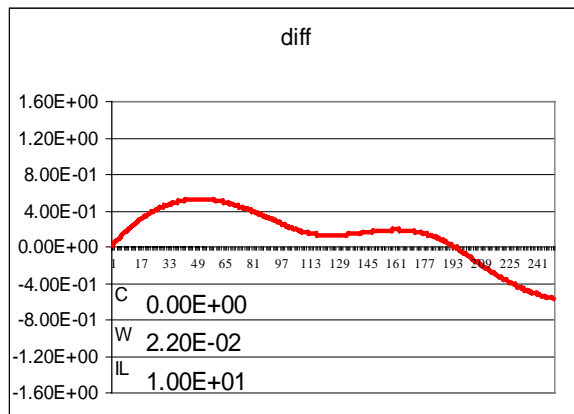
$\phi_{\text{head}} - \phi_{\text{tail}}$ as function of intensity.

Difference between head and tail of batch

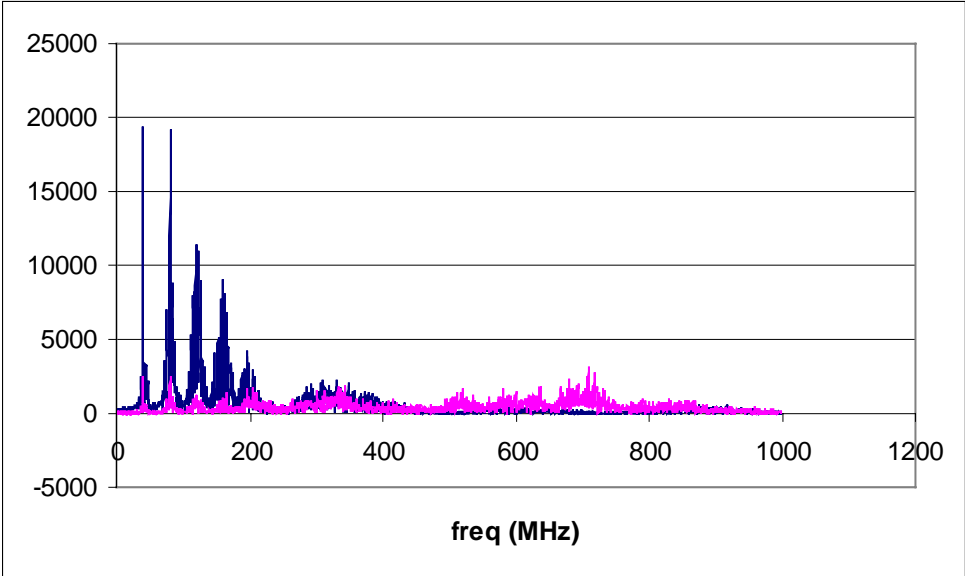
Measurement



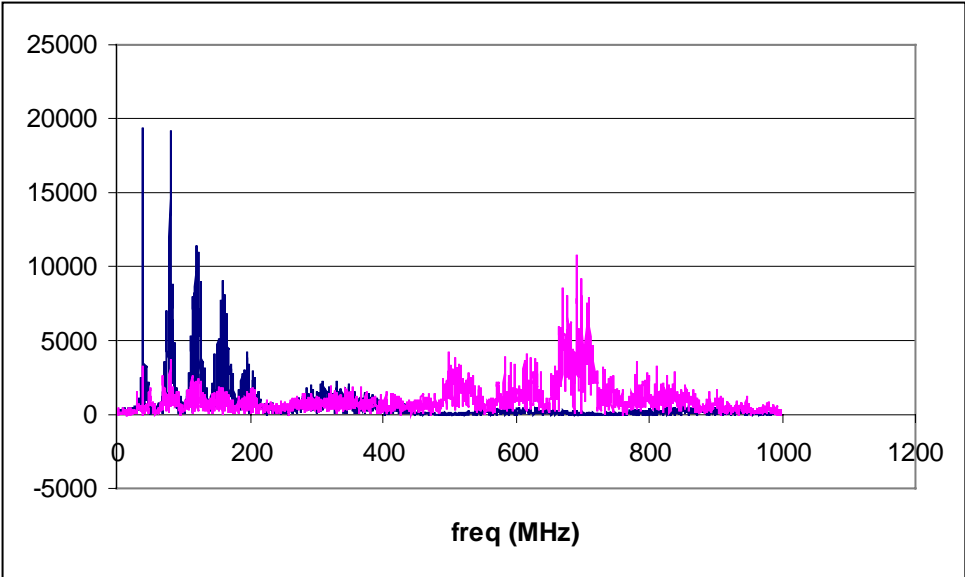
Calculation



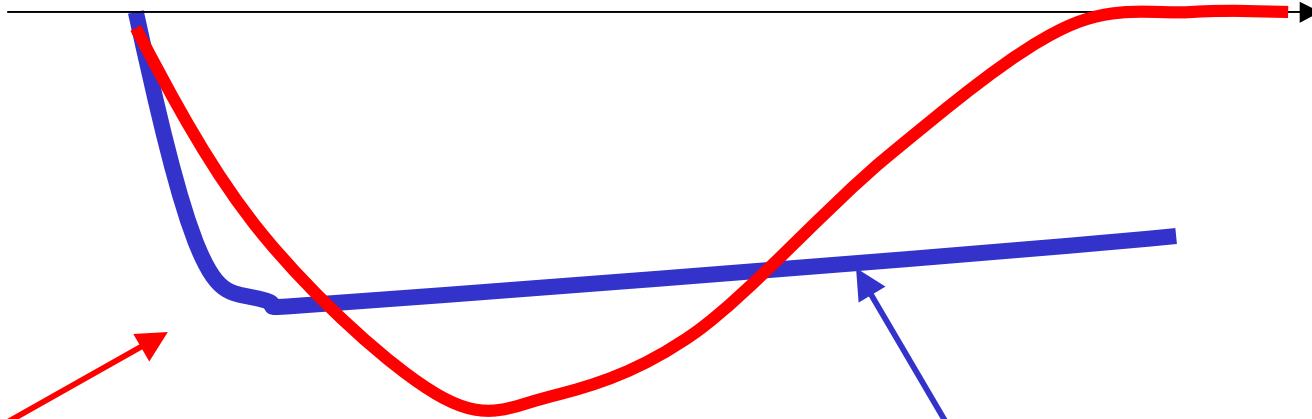
Bunch at beginning of batch



Bunch at the end
Of batch



The Vertical Wakefield



Bunch at the end of batch

Single bunch
Or bunch at the beginning of batch

CONCLUSIONS

- In the SPS the electron cloud is created in the dipoles.
- It results in a fast horizontal coupled bunch instability of low order that can be cured by feedback.
- The vertical instability is of single bunch nature (higher head tail mode). The growth rate depends on intensity.
- The vertical instability seems to be enhanced by a machine impedance 600-800 MHz