



Electron cloud effect for JLC damping ring

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Parameters

- ✦ Energy $E=1.98\text{GeV}$
- ✦ Circumference $L=395\text{m}$
- ✦ Bunch population $N_+=0.75\times 10^{10}$
- ✦ Bunch spacing $L_{\text{sp}}/c=1.4\text{ns}$
- ✦ Bunch train structure $(72\text{bunch}\times 1.4\text{ns}+60\text{ns})\times 4$
- ✦ Total current $I_+=700\text{mA}$
- ✦ Emittance $\epsilon_x=7\times 10^{-10}\text{m}$ $\epsilon_y=5\times 10^{-12}\text{m}$
- ✦ Bunch length $\sigma_z=5\text{mm}$

Electron cloud build-up

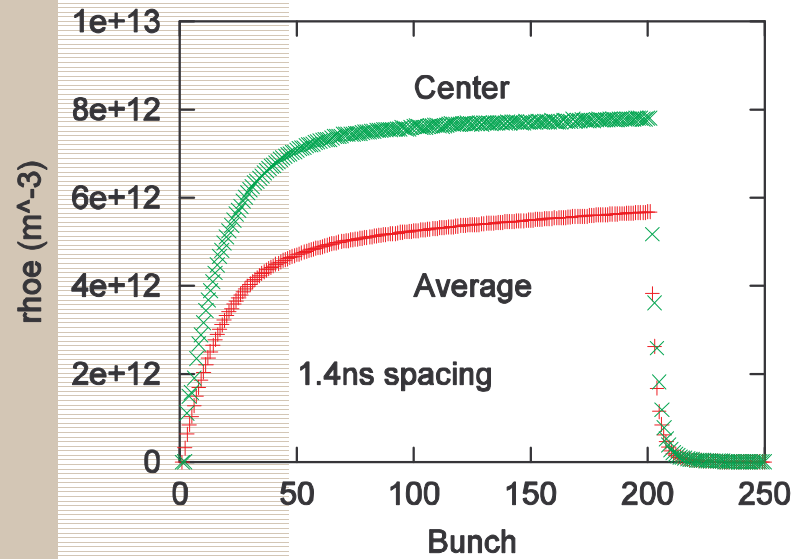
- ✦ Ante-chamber $R=1\text{cm}$
- ✦ In KEKB test ante-chamber, electron current 1/5 of cylindrical chamber was observed.
- ✦ Average Photoelectron yield $Y_{1\gamma}=0.013 \text{ e}^-/(\text{m.e}^+)$ for $Y_{\gamma}=0.65 \text{ } \gamma/(\text{m.e}^+)$.
(KEKB $0.015 \text{ e}^-/(\text{m.e}^+)$ for $Y_{\gamma}=0.15 \text{ } \gamma/(\text{m.e}^+)$)
- ✦ Secondary $Y_2=1.0 \text{ e/e}$
- ✦ The yield approximately corresponds to electron current at surface by

$$I_{ec} (\text{A/m}^2) = Y_{1(+2)} N_p e f_{rep} / 2\pi R$$

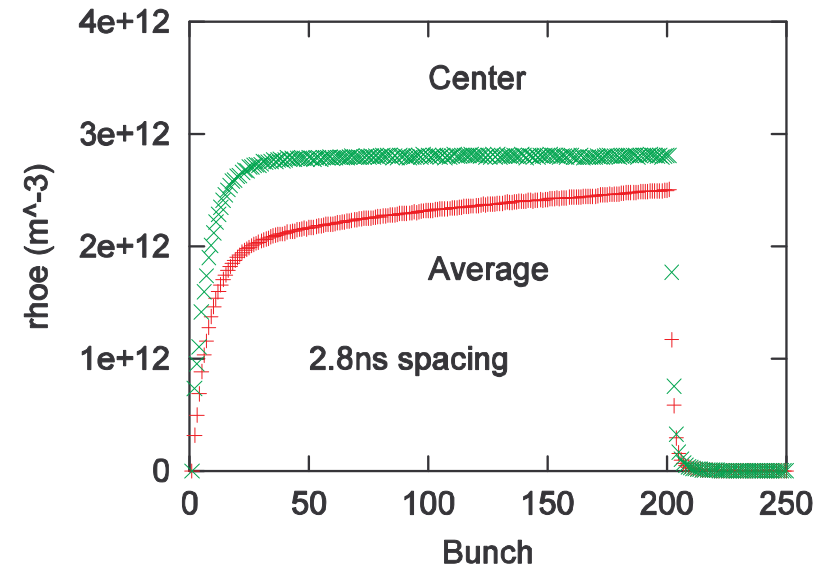
Electron density



1.4ns



2.8ns





Instability caused by electron cloud

- ✖ Coupled bunch instability
- ✖ Single bunch instability
- ✖ We estimate these instabilities by the approximation with the wake force.

Coupled Bunch Instability caused by electron cloud

- ✦ Wake force is calculated a numerical method as follows,
 - Equilibrium electron cloud.
 - A (i-th) bunch Δy_i with a displacement passes through the cloud.
 - Calculate kick $\Delta p_{y,j}$ of j-th bunch.

$$W(z_i - z_j) = \frac{\gamma}{N_p r_e} \frac{\Delta p_{y,j}}{\Delta y_i}$$

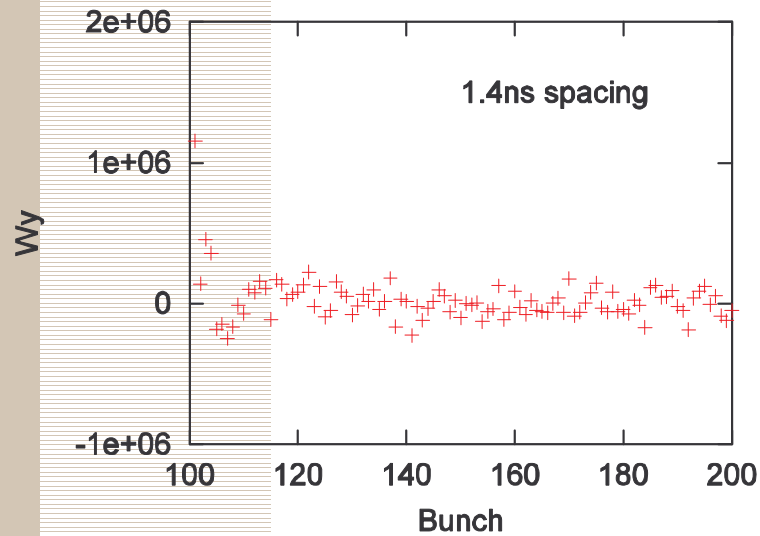
- ✦ Growth of the coupled bunch instability is estimated by

$$\Omega_m - \omega_\beta = \frac{N_\gamma r_e c}{2\gamma T_0 \omega_\beta} \sum_{n=1}^{n_0} W\left(\frac{n}{h} L\right) \exp\left(2\pi i n \frac{m + \nu_y}{h}\right)$$

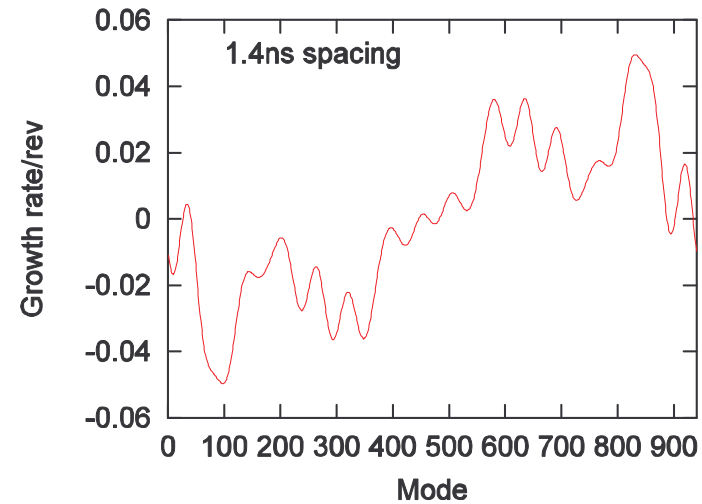
Medium range Wake force and growth of CBI (Fill 1.4ns)



Wake force



Mode stability

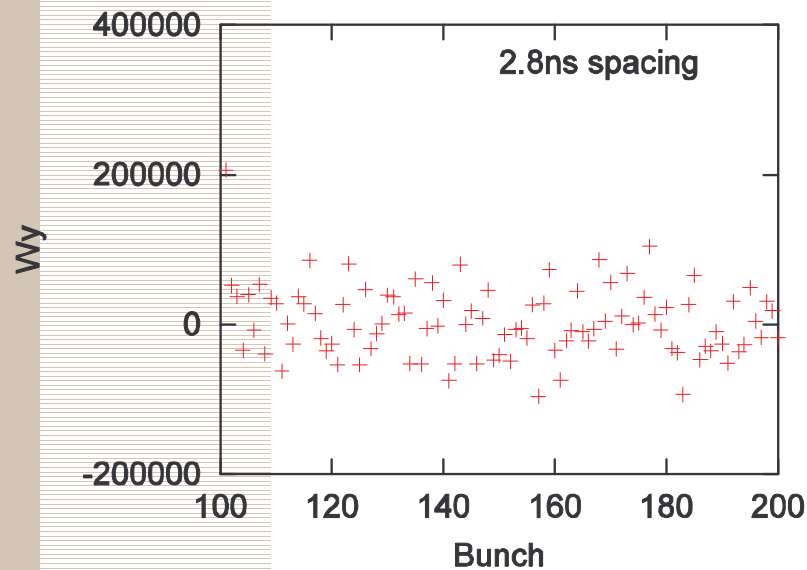


Growth time 20 turns 26 μ s

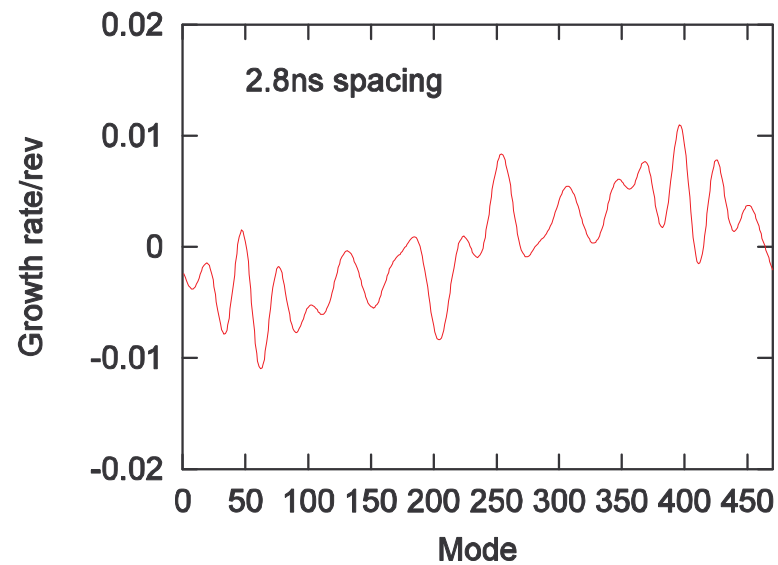
Medium range Wake force and growth of CBI (Fill 2.8ns)



Wake force



Mode stability



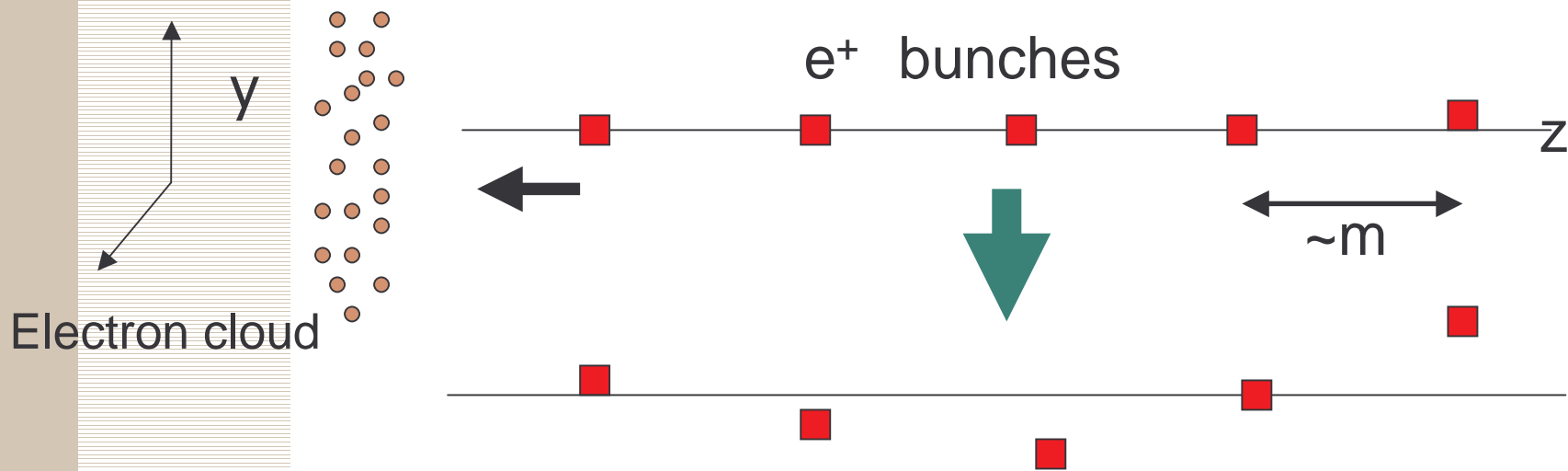
Growth time 100 turns $130\mu\text{s}$

Tracking simulation

Solve both equations of beam and electrons simultaneously

$$\frac{d^2 \mathbf{x}_{+,a}}{ds^2} + K(s) \mathbf{x}_{+,a} = \frac{2r_e}{\gamma} \sum_{j=1}^{N_i} \mathbf{F}_G(\mathbf{x}_{+,a} - \mathbf{x}_{e,j}; \sigma(s)) \delta(s - s_j)$$

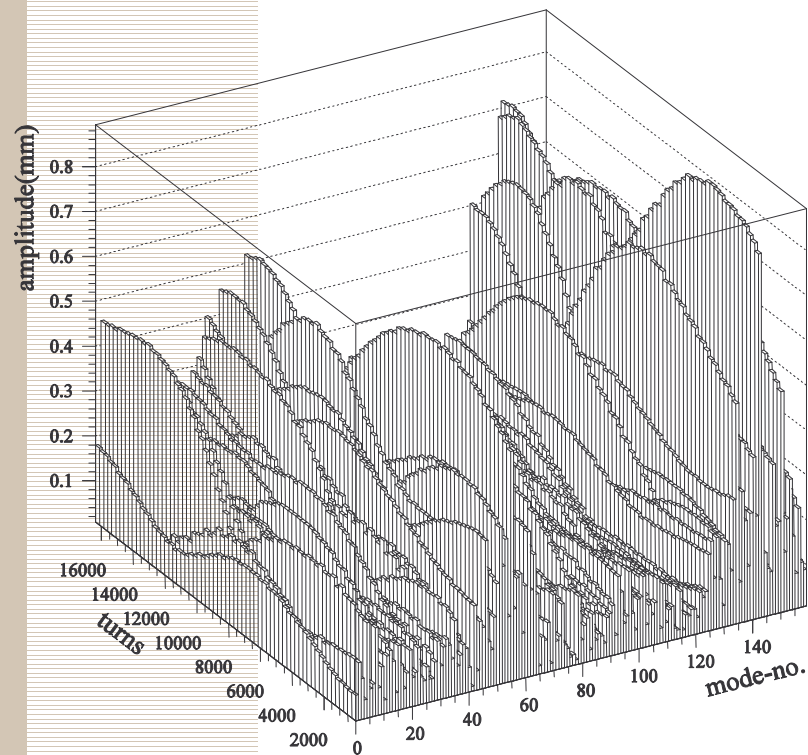
$$\frac{d^2 \mathbf{x}_{e,j}}{dt^2} = 2N_+ r_e c^2 \mathbf{F}_G(\mathbf{x}_{e,j} - \mathbf{x}_{+,a}; \sigma(s)) \delta(t - t(s_{e,j})) - \frac{e}{m} \frac{\partial \phi}{\partial \mathbf{x}}$$



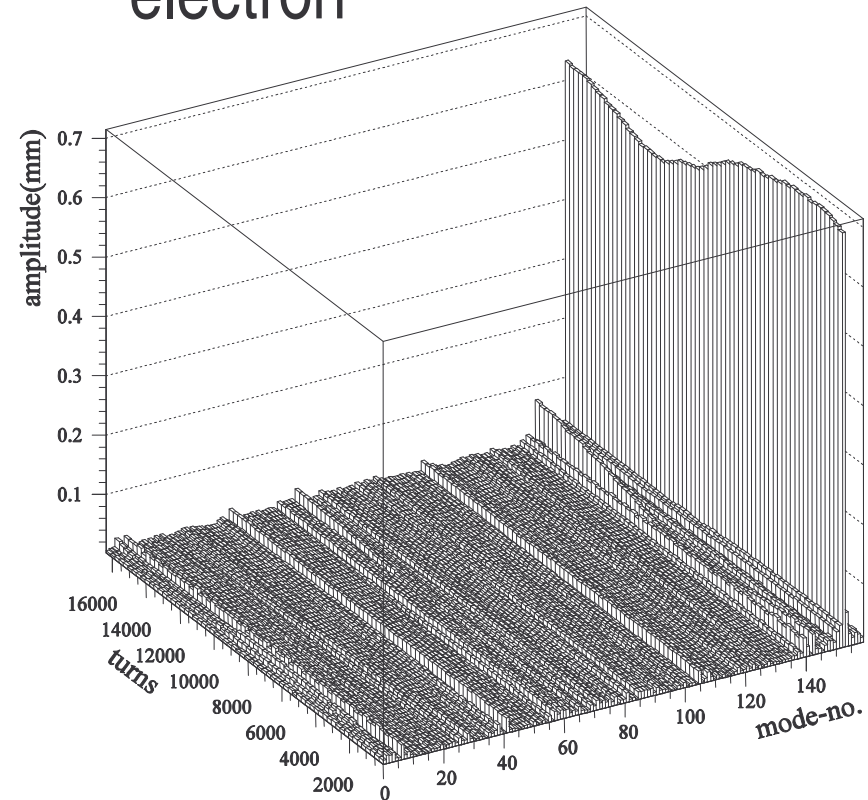
Coupled bunch instability in other rings

BEPC mode spectra by Single Path Beam Position Monitor

Positron



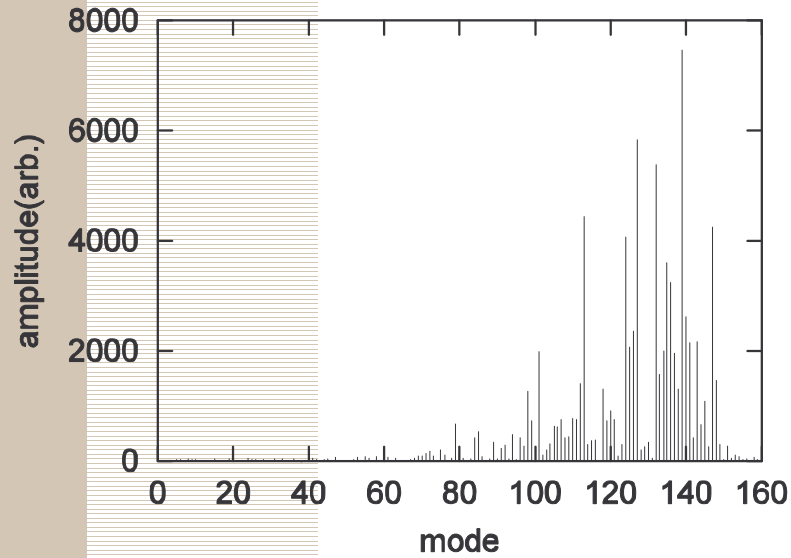
electron



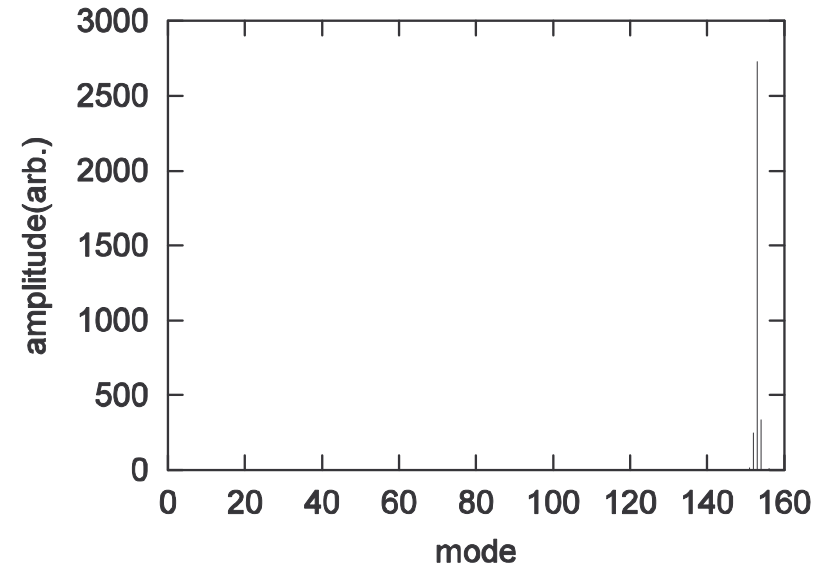


BEPC mode spectra by tracking simulation

Positron



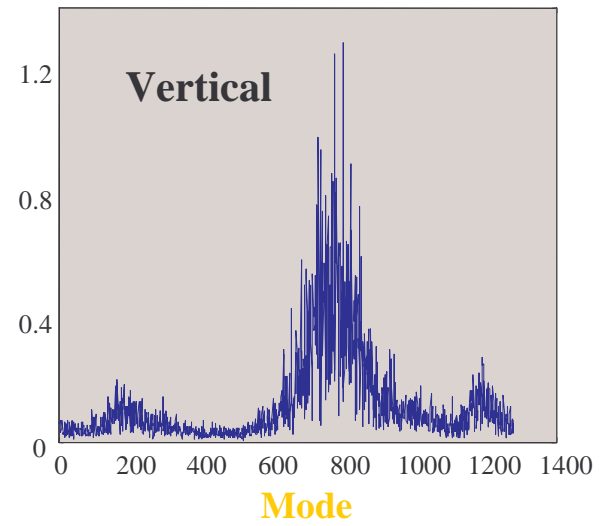
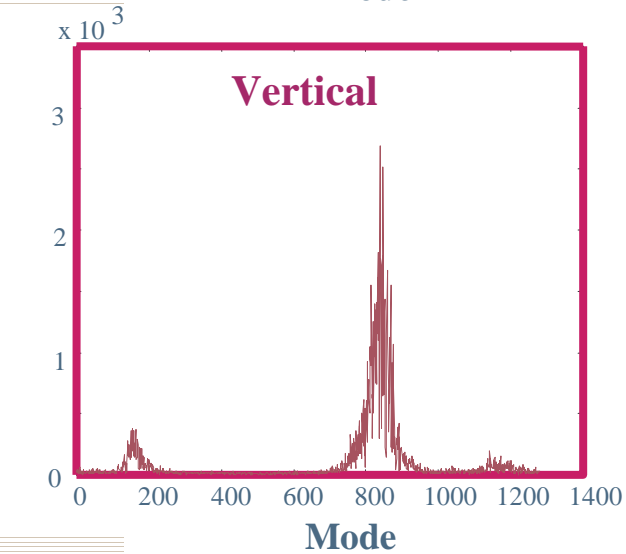
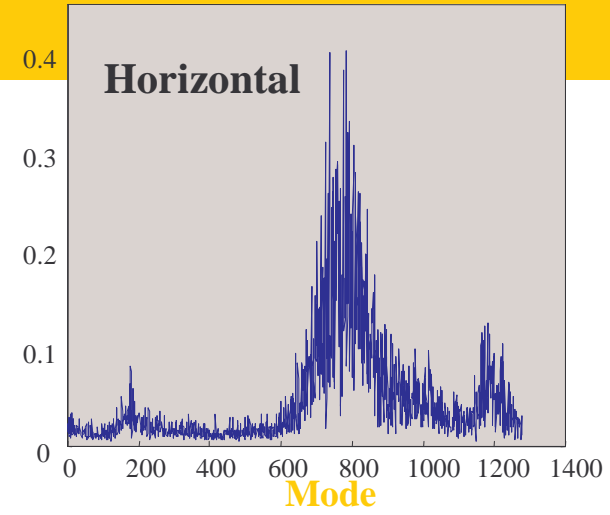
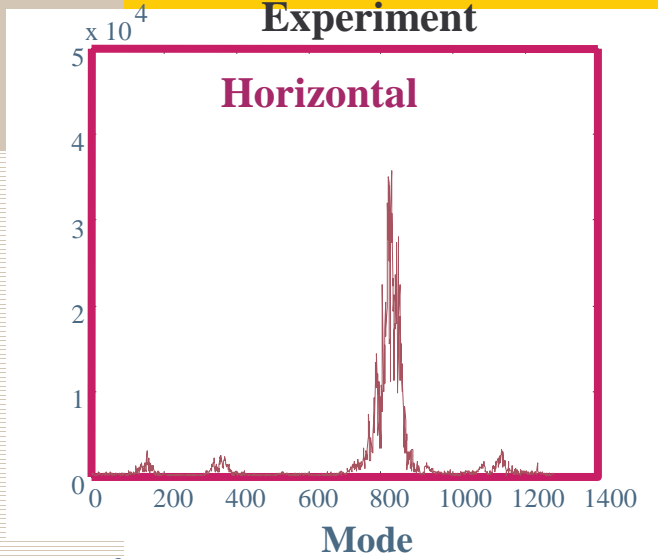
electron



Solenoid-Off

KEKB

Simulation



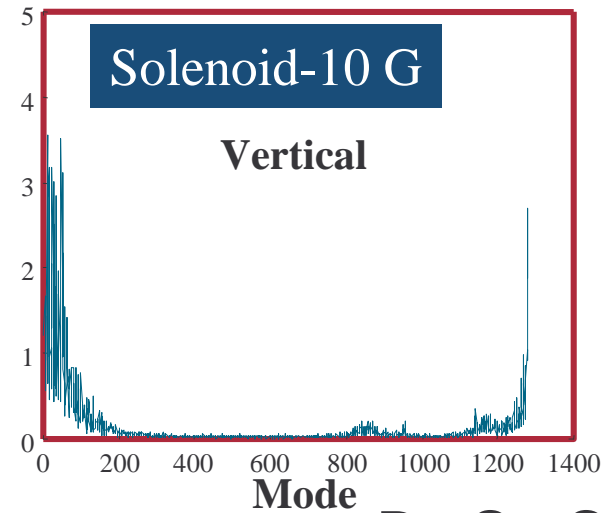
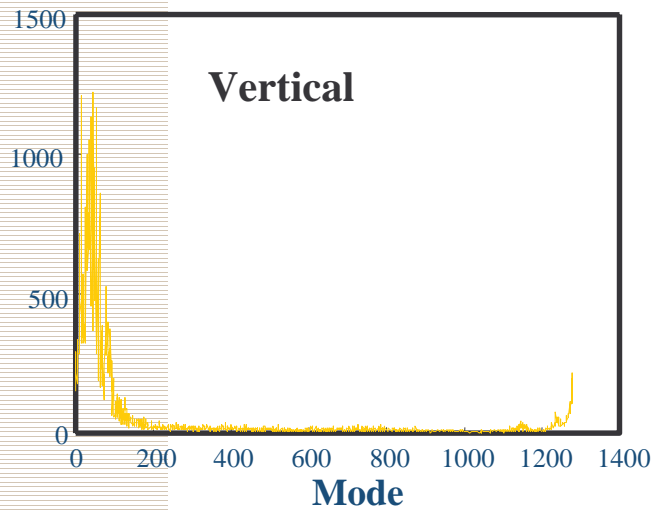
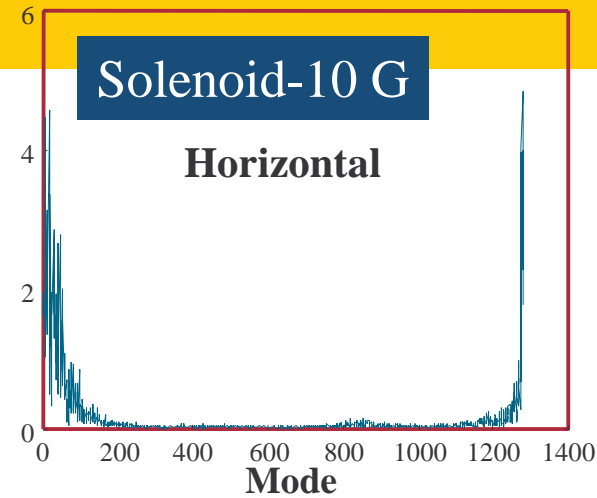
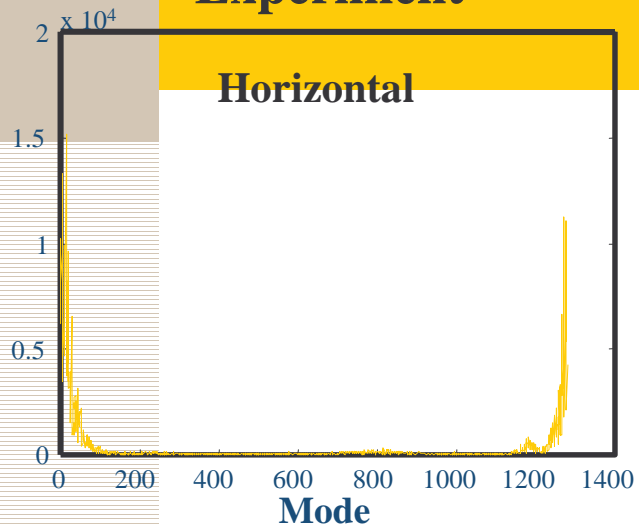
By Su Su Win

Solenoid-ON

KEKB

Experiment

Simulation



By Su Su Win



Single bunch instability caused by electron cloud

- ✦ The single bunch instability is analyzed by wake field method and tracking simulation.

Wake field

- ✦ Linearized model.
- ✦ Numerical calculation including nonlinearity.
(Similar way to the calculation of the multi-bunch wake field)

Short range wake field induced by electron cloud

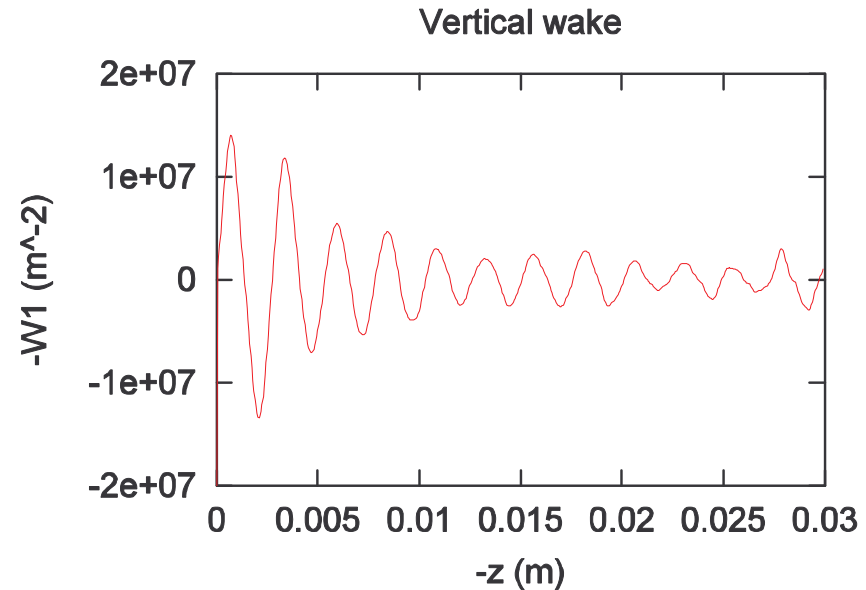
Short range wake for coasting beam

Analytical solution with a simplified linear theory

$$W = K \frac{\lambda_e}{\lambda_p} \frac{L}{(\sigma_x + \sigma_y)\sigma_y} \frac{\omega_e}{c} \sin\left(\frac{\omega_e}{c} z\right)$$

◆ $cR/Q = 1.4 \times 10^7 \text{ m}^{-2}$ ($0.94 \times 10^7 \text{ m}^{-2}$)

◆ $\omega_e =$ ($5.5 \times 10^{11} \text{ s}^{-1}$)



Threshold of fast head-tail instability

- ✦ Bounce frequency of electrons in the positron beam potential

$$\omega_e \sigma_z / c = 9.5 \text{ (V)} \gg 1 \quad 2.6 \text{ (H)} > 1$$

- ✦ Coasting beam model

- ✦ Stability criteria

$$U = \frac{\sqrt{3} \lambda_p r_0 \beta}{v_s \gamma \omega_e \sigma_z / c} \frac{|Z_{\perp}(\omega_e)|}{Z_0} = 1$$

Threshold cloud density of some positron rings

	KEKB	DAFNE	PEPII	JLC DR
E (GeV)	3.5	0.55	3.1	1.98
L (m)	3016	97.7	2000	395
N_p	$3.30E+10$	$4.00E+10$	$6.00E+10$	$7.50E+09$
$\omega \sigma_z / c$	2.5	3.2	3.8	9.1
v_s	0.018	0.012	0.02	0.02
σ_x (μm)	420	2000	800	84
σ_y (μm)	60	63	80	7.1
σ_z (mm)	4	24	12	5
$Z(\rho=10^{12})$	1088	193	1236	826
ρ_{th}	$5.60E+11$	$1.64E+12$	$8.04E+11$	$2.56E+12$

Equation of motion for Gaussian model

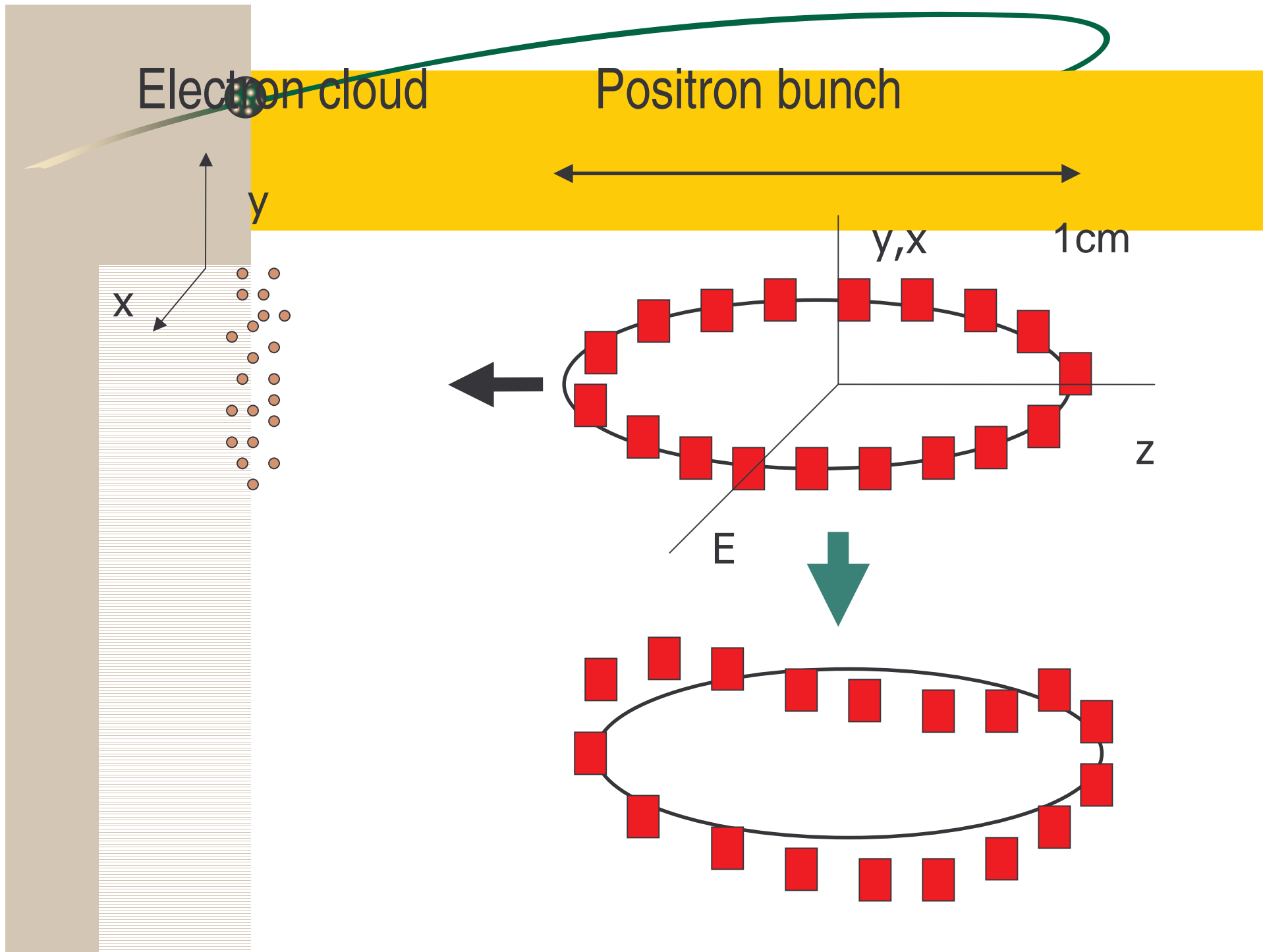
- ✦ Macro-particles with fixed transverse Gaussian size (distributed in the longitudinal phase space).
- ✦ Macro-electrons in transverse plane.

$$\frac{d^2 \mathbf{x}_{+,a}}{ds^2} + K(s) \mathbf{x}_{+,a} = \frac{2r_e}{\gamma} \sum_{j=1}^{N_i} \mathbf{F}_G(\mathbf{x}_{+,a} - \mathbf{x}_{e,j}; \sigma(s)) \delta(s - s_j)$$

$$\frac{d^2 \mathbf{x}_{e,j}}{dt^2} = 2N_+ r_e c^2 \mathbf{F}_G(\mathbf{x}_{e,j} - \mathbf{x}_{+,a}; \sigma(s)) \delta(t - t(s_{+,a}))$$

The same equation as CBI except of the time scale (s~1cm).

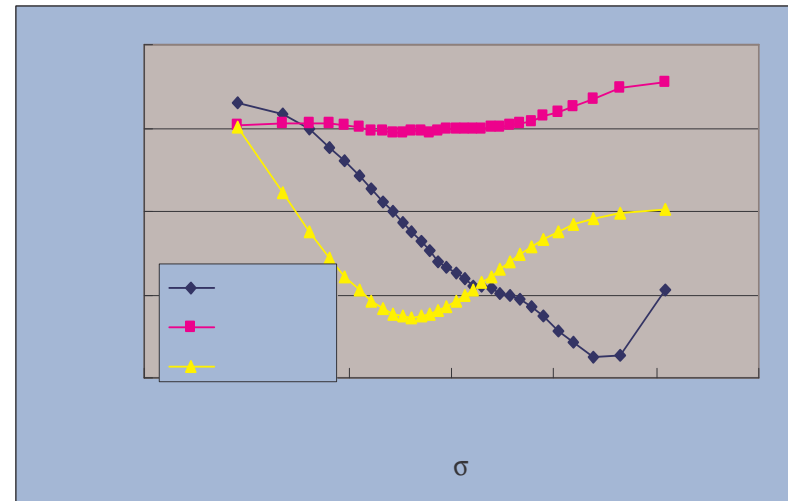
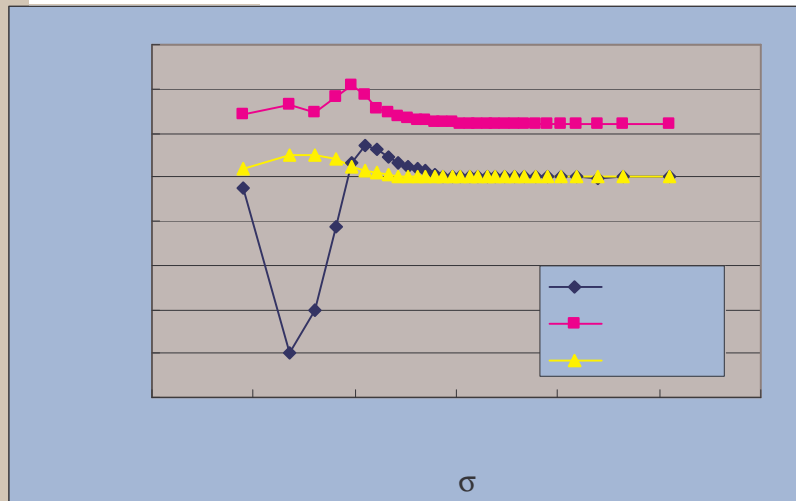
CBI (s~1m)



PIC simulation

- Transverse mesh. 2D electric field calculation for electrons and positron bunch.
- A bunch was sliced into 20-30 in the longitudinal direction.

Snap shot of beam shape for $v_s=0$ and $v_s>0$



KEKB

Summary

- ✦ We assume primary electron yield $Y_{1\gamma} = 0.013 \text{ e}^- / (\text{m.e}^+)$ for JLC damping ring. This value is 1/5 of the direct photoelectron yield, that was measured in KEKB test ante-chamber ($I \sim 1 \text{ A}$).
- ✦ Electron cloud densities are $8 \times 10^{12} \text{ m}^{-3}$ and $3 \times 10^{12} \text{ m}^{-3}$ for 1.4 and 2.8 ns spacing, respectively.
- ✦ The growth of coupled bunch instability is 20 turn ($26 \mu\text{s}$) and 100 turn ($130 \mu\text{s}$) for 1.4 and 2.8 ns spacing, respectively.
- ✦ The growth of 20 turn is serious, but 100 turn can be recovered by bunch by bunch feedback.

Summary (cont.)

- ✖ The threshold cloud density of the fast head-tail instability is $2.5 \times 10^{12} \text{ m}^{-3}$ for $v_s = 0.02$.
- ✖ The wake approximation neglects some effects: nonlinearity, pinching of electrons... A simulation should be performed to confirm the results.
- ✖ We need a factor 3 reduction further for the electron production yield: $Y_{1(+2)} = 0.004 \text{ e}^- / (\text{m.e}^+)$.
- ✖ This value corresponds electron current of $5 \mu\text{A}/\text{cm}^2$ at the chamber surface $R = 1 \text{ cm}$ for beam current $I = 800 \text{ mA}$.
- ✖ It is not impossible to achieve the value.

Summary cont.

Following studies for LC should be done,

- Design of beam chamber. Electron current should be measured in a positron storage ring. ($I_+ = 0.8\text{A}$, $I_{ec} = 1\mu\text{A}$ for $R = 5\text{cm}$ at $Y_\gamma = 0.65 \gamma/(\text{m.e}^+)$), as is done by Harkay et.al.(APS), Macek et.al. (PSR) and Kanazawa et.al.(KEK),
- ATF positron storage with a high current ($\sim 800\text{mA}$).

,if we make progress in LC project with a normal conducting scheme.